Search for or Navigate to? Dual Adaptive Thinking for Object Navigation

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Abstract

"Search for" or "Navigate to"? When we find a specific object in an unknown environment, the two choices always arise in our subconscious mind. Before we see the target, we **search for** the target based on prior experience. Once we have seen the target, we can navigate to it by remembering the target location. However, recent object navigation methods consider using object association mostly to enhance the "search for" phase while neglecting the importance of the "navigate to" phase. Therefore, this paper proposes a dual adaptive thinking (DAT) method that flexibly adjusts thinking strategies in different navigation stages. Dual thinking includes both search thinking according to the object association ability and navigation thinking according to the target location ability. To make navigation thinking more effective, we design a target-oriented memory graph (TOMG) (which stores historical target information) and a target-aware multi-scale aggregator (TAMSA) (which encodes the relative position of the target). We assess our methods based on the AI2-Thor and RoboTHOR datasets. Compared with state-of-the-art (SOTA) methods, our approach significantly raises the overall success rate (SR) and success weighted by path length (SPL) while enhancing the agent's performance in the "navigate to" phase.

1. Introduction

Object navigation [29, 22, 25, 42] is a challenging task that requires an agent to find a target object in an unknown environment with first-person visual observations. Some researchers [31, 15, 19] recently introduced scene prior knowledge into end-to-end navigation networks. These methods have been applied to address various issues, including object associations [39], object attention bias [6], and the lack of universal knowledge [16]. However, these methods improve the efficiency of only the "search for" phase (start—the target is first seen) while neglecting the "navigate to" phase (the target is first seen—end). Our experiments (Table 6 in Appendix B) show that for the current SOTA end-to-end methods, the "navigate to" steps account

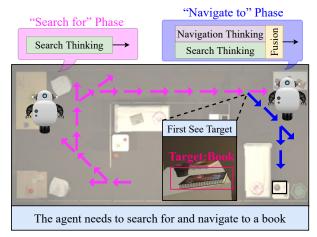


Figure 1. The first target-visible frame divides the agent's navigation process into two phases: "search for" (pink) and "navigate to" (blue). During the "search for" phase, the agent uses only search thinking to search for the target. During the "navigate to" phase, navigation thinking assists the agent in quickly navigating to the target location.

for 62.75% of the whole path, while only 45.78% for humans; the success rate after seeing the target is only 81.09%, while humans can reach 99.92%. Therefore, the primary issue with current end-to-end object navigation techniques is the low navigation efficiency in the "navigate to" phase.

Some modular approaches [5, 32] model the environment by using top-down semantic maps [30, 34]. With the help of detailed semantic maps, the object navigation task can be decoupled into two training subtasks: predicting the subtarget point and navigating to the subtarget point, thus optimizing the agent navigation ability after seeing the target. However, these methods depend strongly on semantic maps, which are hypersensitive to sensory noise and scene changes. Furthermore, generating high-quality semantic maps requires considerable computational resources.

To address the above issues, we aim to integrate this task decoupling concept in modular methods into end-to-end methods. Therefore, we propose the dual adaptive thinking (DAT) method. As shown in Figure 1, the agent's thinking modes are divided into search thinking and navigation

thinking. Search thinking guides the agent to quickly locate the target according to prior knowledge. Navigation thinking assists the agent in efficiently navigating to the target position after locating the target. The agent adaptively adjusts the dominance of the two thinking methods in an end-to-end network according to the navigation progress.

Specifically, we develop different designs for the search thinking network and navigation thinking network. For the search thinking network, we adapt the directed object attention (DOA) graph method proposed in [6] to design object association and attention allocation strategies. For the navigation thinking network, we propose a target-oriented memory graph (TOMG) to store the simplified agent state and target orientation information. Furthermore, we design a target-aware multi-scale aggregator (TAMSA) to refine the features in the TOMG to guide the agent's navigation.

Extensive experiments on the AI2-Thor [20] and RoboTHOR [8] datasets show that our DAT method not only optimizes the "navigate to" phase in the end-to-end network but also outperforms the state-of-the-art (SOTA) method [6] by 8.07% and 8.66% in the success rate (SR) and success weighted by path length (SPL). Moreover, we propose three new metrics, search success rate (SSR), navigation success rate (NSR) and navigation success weighted by navigation path length (NSNPL), to respectively assess the agent's search ability during the "search for" phase and the navigation ability during the "navigate to" phase. As a general concept, the proposed multiple-thinking strategy can be applied in various other embodied artificial intelligence tasks. Our contributions can be summarized as follows:

- We propose a dual adaptive thinking (DAT) method that allows the agent to flexibly use different modes of thinking during navigation.
- We carefully design a navigation thinking network with a selective memory module (TOMG) and a feature refinement module (TAMSA) to implicitly encode the target location into the end-to-end network.
- We demonstrate that our DAT method not only addresses inefficiencies in the "navigate to" phase but also substantially outperforms existing object navigation models.

2. Related Works

2.1. Object Navigation

Object navigation tasks [3, 37, 35] require an agent to navigate to a target object in an unknown environment while considering only visual inputs. Recently, the relationships between objects have been introduced into navigation networks, allowing agents to locate targets more quickly by

considering object associations. Zhang et al. [41] proposed the hierarchical object-to-zone (HOZ) graph to guide an agent in a coarse-to-fine manner. Moreover, Dang et al. [6] utilized a directed object attention (DOA) graph to address the object attention bias problem. These works allow agents to locate targets faster but do not address how to navigate to these targets more quickly. Our dual adaptive thinking (DAT) method divides agents' thinking into two types: search thinking and navigation thinking, which can collaborate adaptively to make every navigation stage efficient.

2.2. Modular Navigation

Modular navigation methods [5, 32] have been proposed to solve the generalizability problem of end-to-end models in complex environments. It has been proven that using a top-down semantic map to predict distant subgoal points [5] is feasible on the Habitat dataset. The PONI [32] method trains two potential function networks by using supervised learning to determine where to search for an unseen object. These modular methods require considerable computing and storage resources to generate semantic maps in real time and are sensitive to image segmentation quality. Our method implicitly incorporates different thinking during navigation into an end-to-end network without relying on semantic maps.

3. Necessity of Dual Thinking

3.1. Dual Thinking in Humans

Embodied AI [12] is a challenging research topic that requires agents to use well-developed intuitive tasks (e.g., classification [36] and detection [24]) to complete complex logical tasks (e.g., navigation [43] and interaction [33]) in real-world environments. Humans often use multiple ways of thinking when completing these complex logical tasks. For example, when we need an object, we first use associative thinking to locate the object and then use navigational thinking to reach the object location; when we answer a question about an object, we first use exploratory thinking to fully understand the object and then use reasoning and language-organized thinking to draw conclusions. Therefore, multiple thinking approaches can be introduced in end-to-end networks to develop interpretable hierarchical models that are more consistent with how humans address complex logic problems.

3.2. Repeated Target Search Problem

In current methods, if the agent loses the target in view, the target must still be searched for again to locate it. Consequently, the agent wastes considerable time in re-searching for the target, potentially leading to constant loops. This problem is especially common in environments with many obstacles. A clear orientation memory for the target is the

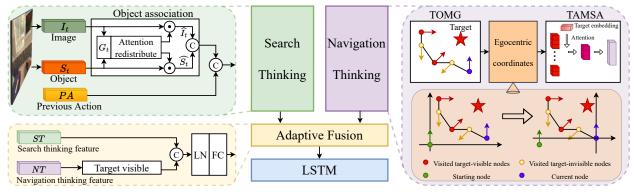


Figure 2. Model overview. TOMG: target-oriented memory graph. TAMSA: target-aware multi-scale aggregator. Our model includes three modules: search thinking, navigation thinking and adaptive fusion. In the search thinking network, we endow the model with an object association ability according to the directed object attention (DOA) graph method proposed in [6]. In the navigation thinking network, we provide the model with the ability to remember the target orientation. In the adaptive fusion network, we make the dual thinking work in harmony according to the navigation progress.

key to solve this problem. Therefore, we design a targetoriented memory graph (TOMG) and a target-aware multiscale aggregator (TAMSA) in the navigation thinking network to ensure that the agent navigates to the target efficiently without repeatedly re-searching.

4. Dual Adaptive Thinking Network

Our goal is to endow agents with both search and navigation thinking and to adjust their status based on the navigation process. To achieve this goal, we design three networks, as illustrated in Figure 2: (i) search thinking network; (ii) navigation thinking network; (iii) adaptive fusion network. (i) and (ii) are connected by (iii) to form the dual adaptive thinking (DAT) network.

4.1. Task Definition

The agent is initialized to a random state $s = \{x, y, \theta, \beta\}$ and random target object p. Here, (x, y) represents the coordinates of the agent, (θ, β) represents the yaw and pitch angles of the agent. At each timestamp t, according to the single view RGB image o_t and target p, the agent learns a navigation strategy $\pi(a_t|o_t,p)$, where $a_t \in A =$ {MoveAhead; RotateLeft; RotateRight; LookDown; LookUp; Done and Done is the output if the agent believes that it has navigated to the target location. Ultimately, if the agent is within a threshold (i.e., 1.5 meters [10]) of the target object when Done is output, the navigation episode is considered successful.

4.2. Search Thinking Network

Search thinking aims to enable the agent to quickly capture the target with the fewest steps when the target is not in view. To use efficient object association, we adopt the unbiased directed object attention (DOA) graph method proposed in [6]. As shown in the green box in Figure 2, accord-

ing to the object-target association score G_t calculated by the DOA method, we redistribute the attention to the object features S_t (from DETR [4]) and image features I_t (from ResNet18 [17]) to ensure that the agent pays attention to objects and image regions that are more relevant to the target.

In the object attention redistribution process, the objecttarget association score of each object q is multiplied by the object features S_t to generate the final object embedding S_t :

$$\widehat{S}_t^q = S_t^q G_t^q \qquad q = 1, 2, \cdots, N \tag{1}$$

 $\widehat{S}_t^q = S_t^q G_t^q \qquad q = 1, 2, \cdots, N \tag{1}$ where $\widehat{S}_t = \{\widehat{S}_t^1, \widehat{S}_t^2, \cdots, \widehat{S}_t^N\}$, and N is the number of

In the image attention redistribution process, we assign attention to image features I_t according to the object semantic embeddings generated by the one-hot encodings. Initially, the semantic embeddings are weighted by $G_t \in$ $\mathbb{R}^{N\times 1}$ to obtain the attention-aware object semantics D. We use D as the query and I_t as the key and value in the multihead image attention to generate the final image embedding

$$Q_i = DW_i^Q \ K_i = I_t W_i^K \ V_i = I_t W_i^V \ i = 1, \cdots, NH$$
 (2)

$$head_{i} = softmax(\frac{Q_{i}K_{i}^{T}}{\sqrt{HD}})V_{i}$$
 (3)
$$\widehat{I}_{t} = Concat(head_{1}, \cdots, head_{NH})W^{O}$$
 (4)

$$\widehat{I}_t = Concat(head_1, \cdots, head_{NH})W^O$$
 (4)

where HD and NH denote the hidden dimensionality and number of heads in the multi-head attention.

Finally, the attention-aware object features S_t and image features I_t are concatenated with the previous action embedding PA to obtain the output ST of the search thinking network.

4.3. Navigation Thinking Network

Target-Oriented Memory Graph (TOMG) Different from search thinking, navigation thinking requires the abil-

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ity to memorize, locate and navigate to the target. Thus, we design a target-oriented memory graph (TOMG) as the input feature M. There are two types of nodes in the history route map (see the purple box in Figure 2): (i) visited target-visible nodes • where the agent detects the target in view; (ii) visited target-invisible nodes \bigcirc where the agent does not detect the target in view. Navigation thinking only focuses target-related information; thus the TOMG is composed of the visited target-visible nodes. Previous historical memory methods [14, 44] which store both the images $m_i \in \mathbb{R}^{7 \times 7 \times 512}$ and objects $m_o \in \mathbb{R}^{N \times 256}$ features contain too much redundant noise. In contrast, our TOMG node only stores high-level features $m \in \mathbb{R}^{1 \times 9}$ which is concatenated by three parts: the target bounding box, the target confidence and the agent's coordinates. By eliminating redundant inputs, our target-oriented storing method uses $3000 \times$ less storage than previous methods [14, 44].

Since the agent cannot obtain its own absolute position and orientation in unknown environments, the stored coordinates $(x_i, y_i, \theta_i, \beta_i)$ are calculated relative to the starting coordinate $(x_0,y_0,\theta_0,\beta_0)$. Target-visible nodes are filtered by a confidence threshold cf of target recognition. Finally, to ensure the reliability of target orientation prediction, only the L closest target-visible nodes to the current node in the path are stored.

Egocentric Coordinate Transformation As the agent navigates during each step, the decisions (e.g., rotate right) are made relative to the current agent's own coordinate system. Therefore, before using the TOMG features, we convert the coordinates of each node in the TOMG to the coordinate system of the current node $(x_c, y_c, \theta_c, \beta_c)$ (see the orange box in Figure 2):

$$(\widetilde{x}_{i}, \widetilde{y}_{i}) = (x_{i}, y_{i}) - (x_{c}, y_{c})$$

$$(\widetilde{\theta}_{i}^{x}, \widetilde{\beta}_{i}^{x}) = \sin((\theta_{i}, \beta_{i}) - (\theta_{c}, \beta_{c}))$$

$$(\widetilde{\theta}_{i}^{y}, \widetilde{\beta}_{i}^{y}) = \cos((\theta_{i}, \beta_{i}) - (\theta_{c}, \beta_{c})) \quad i \in \Delta_{M}$$

$$(5)$$

where Δ_M represents the index collection of target-visible nodes. To ensure that the angle and position coordinates have the same order of magnitude, we use sin and costo normalize the angle coordinates to [-1,1]. After this egocentric coordinate transformation, we obtain egocentric TOMG features $\widetilde{M} \in \mathbb{R}^{L \times 11}$.

Target-Aware Multi-Scale Aggregator (TAMSA) encode navigation thinking into the network, we design a target-aware multi-scale aggregator (TAMSA) to aggregate the egocentric TOMG feature M into an implicit representation NT. In contrast to typical methods that use transformers or temporal convolutions as encoders, we devise a unique dynamic encoder that better leverages the memory graph features, as described below.

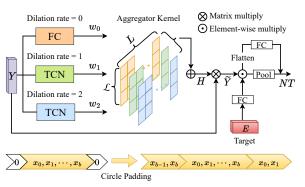


Figure 3. A detailed explanation of the target-aware multi-scale aggregator (TAMSA). We first use the multi-scale TCNs to obtain aggregator kernels that aggregate the target-oriented memory graph (TOMG) with L nodes into graph with \pounds nodes. Then, the aggregated features allocate attention to the channel dimension using the target semantics. We describe the circle padding method applied in our TCNs below the figure.

First, to improve the feature expression ability of the navigation thinking network, we use fully connected (FC) layers to map the features M to higher dimensional spaces. Inspired by some advanced works [9, 26] on vision transformers, we add layer normalization between the two FC layers to stabilize the forward input distribution and backpropagation gradient [38]. The encoding details can be formulated as follows:

$$Y = \delta(LN(\widetilde{M}W^{M_1})W^{M_2}) \tag{6}$$

where δ denotes the ReLU function, LN denotes layer normalization, and $W^{M_1} \in \mathbb{R}^{11 \times 16}$ and $W^{M_2} \in \mathbb{R}^{16 \times 32}$ are learnable parameters.

Then, a multi-scale dynamic kernel is calculated to refine the target orientation features into implicit nodes. As shown in Figure 3, we use three temporal convolution networks (TCNs) with different dilation rates d to generate three dynamic kernels with distinct scales. It is worth noting that the TCN with d=0 degenerates to an FC layer. In the early stages of the "navigate to" phase, the TOMG contains fewer valid nodes; thus, the boundary degradation caused by zero padding has a greater impact. To avoid padding with zero, inspired by [40], we design the circle padding (CP) which fills the sequence edge with the features at the other end of the sequence (Figure 3). The different scale kernels are added after multiplying by the learnable parameter w_d :

$$H(l) = \sum_{d=0}^{2} w_d (\sum_{j \in \Psi} Y(l+j*d) * f_d(j) + b_d)$$
 (7)

where $H = \{H(1), \dots, H(L)\}, l$ is the central node of the convolution kernel. Ψ refers to the set of offsets in the neighborhood considering convolution conducted on the central node, $Y(\cdot)$ takes out the node features in Y, and

Table 1. Ablation results on each module in the three sub-networks: search, navigate and fusion.

ID	Search T	hinking	Na	vigation Thin	king	Fus	sion			ALL (%)		Episode
	Associate	Pretrain	TOMG	Egocentric	TAMSA	AF	LN	SR↑	SPL↑	SSR↑	NSR↑	NSNPL↑	Time (s)↓
1								71.34	40.36	92.41	76.19	43.74	0.258
2	✓							74.43	40.93	95.82	77.67	44.11	0.334
3	✓	\checkmark						76.78	43.88	94.19	81.40	47.09	0.334
4	✓	✓	√					76.02	43.15	93.41	80.21	47.12	0.336
5	✓	\checkmark	\checkmark	\checkmark				78.12	42.01	95.12	82.13	45.80	0.336
6	✓	\checkmark	\checkmark		\checkmark			78.04	45.67	94.83	82.29	48.44	0.345
7	✓	\checkmark	\checkmark	\checkmark	\checkmark			80.88	45.71	95.46	84.72	48.31	0.346
8	✓	✓	√	√	√	√		81.34	47.53	96.38	84.39	49.74	0.350
9	✓	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	82.39	48.93	97.25	84.71	50.32	0.352

 f_d and b_d denote the weights and biases in the convolution kernel with dilation rate d. The multi-scale dynamic kernel $H \in \mathbb{R}^{L \times \pounds}$ refines $Y \in \mathbb{R}^{L \times 32}$ to $\widetilde{Y} \in \mathbb{R}^{\pounds \times 32}$.

Intuitively, the mappings between the observation data and target azimuth differ when searching for different targets. For example, when looking for a TV, even if the TV is located far from the agent, the agent can clearly identify the target and obtain a larger target bounding box; however, when looking for a mobile phone, the agent can only obtain a smaller target bounding box, even if the agent is close to the mobile phone. Therefore, we enhance the TAMSA representation by considering the target semantic information. To achieve this goal, the one-hot target index E is encoded to the same channel dimension as \widetilde{Y} through two FC layers, whose result is channel-wise multiplied with \widetilde{Y} to get the target-aware feature representation \widehat{Y} :

$$\widehat{Y} = H^T Y \odot \delta(\delta(EW^{E_1})W^{E_2}) \tag{8}$$

Finally, to obtain the final output NT of the navigation thinking network, we flatten \widehat{Y} from $\mathbb{R}^{\pounds \times 32}$ to $\mathbb{R}^{1 \times 32 \pounds}$ and use an FC layer to reduce the output dimension. Furthermore, we add residual connections to ensure the stability of the feature transfer process.

$$NT = \delta(Flatten(\widehat{Y})W^{Y}) + \frac{1}{\mathcal{L}} \sum_{l=1}^{\mathcal{L}} \widehat{Y}(l)$$
 (9)

A dropout layer is added before the output to reduce overfitting in the navigation thinking network.

4.4. Adaptive Fusion (AF) of Dual Thinking Networks

Search thinking and navigation thinking have different work strategies according to the navigation progress. During the "search for" phase, since there are no visited target-visible nodes, NT is an all-zero matrix. Therefore, the navigation thinking network does not affect the action decision when the target has not yet been seen. During the "navigate to" phase, to ensure navigation robustness, search thinking and navigation thinking work together to guide the action

decision. As the number of visited target-visible nodes increases, navigation thinking gradually dominates. The fusion process of the two thinking methods can be expressed

$$DT = (LN(Concat(NT, ST)))W$$
 (10)

where W is a learnable parameter matrix that adaptively adjusts the proportion of the two thinking networks, and LN is demonstrated to be significantly beneficial to the generalizability of the model.

Finally, the dual adaptive thinking output DT is used to learn an LSTM [18] action policy $\pi(a_t|DT_t,p)$.

4.5. Policy Learning

Following the previous works [27, 13], we treat this task as a reinforcement learning problem and utilize the asynchronous advantage actor-critic (A3C) algorithm [28]. However, in the search thinking network, the complex multi-head attention calculations are difficult to directly learn by reinforcement learning [11]; thus, we use imitation learning to pretrain the search thinking network. We divide the continuous action process into step-by-step action predictions and teach the agent to rely on only object associations to determine actions without considering historical navigation information. After pretraining, we obtain a search thinking network with a basic object association ability. Finally, the search thinking network and the navigation thinking network are jointly trained via reinforcement learning.

5. Experiment

5.1. Experimental Setup

Datasets AI2-Thor [20] is our main experimental platform, which includes 30 different floorplans for each of 4 room layouts: kitchen, living room, bedroom, and bathroom. For each scene type, we use 20 rooms for training, 5 rooms for validation, and 5 rooms for testing. Additionally, we employ the RoboTHOR [8] dataset, which has 2.4 times larger area and 5.5 times longer trajectory length than AI2-Thor.

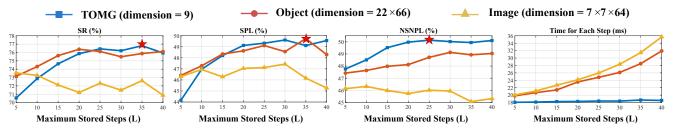


Figure 4. We compare the metrics in paths with $\mathbb{L} \geq 5$ while storing different features and path lengths for navigation thinking. The red five-pointed star indicates the choices that optimize the given indicator.

Evaluation Metrics We use the success rate (SR) and success weighted by path length (SPL) [1] metrics to evaluate the overall performance of our method. Our proposed matrics, search success rate (SSR), navigation success rate (NSR) and navigation success weighted by navigation path length (NSNPL), are used to clearly reflect the agent's ability in the "search for" phase and "navigate to" phase.

SR is formulated as $SR = \frac{1}{F} \sum_{i=1}^{F} Suc_i$, where F is the number of episodes and Suc_i indicates whether the i-th episode succeeds. SPL considers the path length more comprehensively and is defined as $SPL = \frac{1}{F} \sum_{i=1}^{F} Suc_i \frac{\mathbb{L}_i^*}{max(\mathbb{L}_i, \mathbb{L}_i^*)}$, where \mathbb{L}_i is the path length taken by the agent and \mathbb{L}_i^* is the theoretical shortest path.

SSR is the success rate for the "search for" phase and is formulated as $SSR = \frac{1}{F} \sum_{i=1}^F Nav_i$, where Nav_i indicates whether the *i*-th episode enters the "navigate to" phase. NSR is the success rate for the "navigate to" phase and is formulated as $NSR = \frac{1}{FNav} \sum_{i=1}^F Suc_i Nav_i$, where F_{Nav} is the number of episodes that enter the "navigate to" phase. NSNPL considers the navigation efficiency during the "navigate to" phase and is defined as:

$$NSNPL = \frac{1}{F_{Nav}} \sum_{i=1}^{F} Suc_i Nav_i \frac{\mathbb{L}_i^{*Nav}}{max(\mathbb{L}_i^{Nav}, \mathbb{L}_i^{*Nav})}$$
(11)

where \mathbb{L}_i^{Nav} is the path length in the "navigate to" phase and \mathbb{L}_i^{*Nav} is the theoretical shortest path length in the "navigate to" phase. During testing, we calculate \mathbb{L}_i^{*Nav} in real time according to the starting position of the "navigate to" phase (the position where the agent first recognizes the target) in each task path. Intuitively, NSNPL can be conceptualized as the SPL of "navigate to" phase.

Implementation Details We train our model with 18 workers on 2 RTX 2080Ti Nvidia GPUs. The dropout rate and target-visible filter cf in our model are set to 0.3 and 0.4, respectively. The number of implicit nodes \pounds in TAMSA is set to 3. We report the results for all targets (ALL) and for a subset of targets ($\mathbb{L} \geq 5$) with optimal trajectory lengths greater than 5. More network details are given in Appendix A.

Table 2. Ablation experiments on each module in the target-aware multi-scale aggregator (TAMSA). Dynamic: dynamic aggregator kernel, TA: target-aware, MS: multi-scale, CP: circle padding.

	/letho	.d	ALL (%)									
	vietno	ou	SR↑	SPL↑	SSR↑	NSR↑	NSNPL↑					
Avera	ige P	ooling	79.67	45.14	97.29	81.88	47.89					
Tra	nsfor	mer	77.23	43.24	96.31	80.06	46.34					
	TCN	Ī	78.66	43.41	96.16	81.52	46.61					
	A1	Dynamic	80.15	44.26	97.04	82.59	47.31					
	A2	A1+TA	81.20	46.71	97.17	83.56	48.93					
TAMSA	A3	A1+MS	81.14	47.28	96.93	83.64	49.51					
	A4	A2+MS	81.32	47.41	97.42	83.47	49.28					
	A5	A4+CP	82.39	48.93	97.25	84.71	50.32					

5.2. Ablation Experiments

Baseline Similar to [10, 41, 6], our baseline model adopts the features concatenated from the image branch (from ResNet18 [17]), object branch (from DETR [4]) and previous action branch as the environment perception encoding. Next, an LSTM network is used to model the temporal implicit features. The first row in Table 1 shows the performance of our baseline.

Dual Thinking As shown in Table 1, the model with search thinking outperforms the baseline with the gains of 5.44% and 3.52% in SR and SPL. The search thinking network enables the agent to quickly locate the object through object associations. Incorporating our proposed navigation thinking directly improves the NSR and NSNPL by 3.32% and 1.22%, demonstrating that the navigation thinking improves the agent's navigation ability after seeing the target.

Navigation Thinking Network The navigation thinking network includes three key modules: the target-oriented memory graph (TOMG), the egocentric coordinate transformation module and the target-aware multi-scale aggregator (TAMSA). Rows 4 through 7 in Table 1 show the ablation results on the three modules. The navigation thinking network without the TAMSA increases the SR by 1.34% but decreases the SPL by 1.87%. TAMSA improves the SPL back by refining the introduction of navigation thinking.

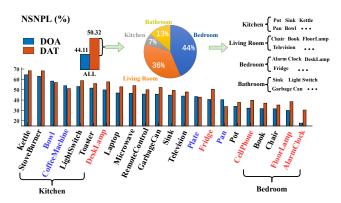


Figure 5. Compare the NSNPL of DOA[6] method and our propose DAT method target-by-target on the AI2-Thor. After using the DAT method, red target objects improve significantly and blue target objects decrease. Pie chart summarizes the contributions of all scenes. The right side of the pie chart shows common objects in each scene.

The simplified and highly abstract storage features in the TOMG facilitate the subsequent feature refinement and thinking integration. Figure 4 displays various metrics and computation speeds while using different storage features (TOMG, object and image) and maximum stored steps L. Image features perform the worst. Compared with object features, our TOMG considerably improves the NSNPL. Most importantly, the TOMG is substantially less complex than other storage methods. In terms of computational efficiency, when the number of stored steps is set to 40, compared with storing object and image features, the TOMG improves the computational speed by 41.43% and 47.69%, respectively. In terms of memory usage, the TOMG requires only 0.64% and 0.29% of the memory required by the object and image features. Furthermore, as the number of stored steps increases, the computational burden of the TOMG storage method remains essentially constant.

Target-Aware Multi-Scale Aggregator (TAMSA) Our proposed TAMSA uses a dynamic kernel to achieve auto-

matic sequence length reduction without applying global pooling at the end. As shown in Table 2, the use of either TCNs or transformers exhibits worse performance than using average pooling directly. This finding suggests that our navigation thinking network is incompatible with these widely used encoders. Based on the initial aggregator model (A1), the target-aware (TA) property brings improvements of 0.97%, 1.62%, and the multi-scale (MS) property brings improvements of 1.05%, 2.20% in NSR and NSNPL. Furthermore, we utilize circle padding (CP) to prevent serious information loss in limited target-visible nodes, thereby optimizing the path during short-distance navigation.

Fusion of Dual Thinking Modules Our proposed adaptive fusion module (rows 8 and 9 in Table 1) effectively integrates the two separately designed thinking networks and improves the SR, SPL and SSR metrics by 1.51%, 3.22% and 1.79%. Fundamentally, adaptive fusion and layer norm decouple diverse thinking and increase the specificity of varied thinking.

5.3. Comparative Analysis of Different Targets

Figure 5 visualizes the NSNPL for different targets using the DOA [6] model and our DAT model. Obviously, the objects with the highest NSNPL belong to the kitchen scene, and the objects with the lowest NSNPL belong to the bedroom scene. The bedroom has more complex obstacles than the kitchen, which leads to the gap in difficulty of the "navigate to" phase. The NSNPL of most objects has improved thanks to our DAT method, notably those in the intricate bedroom scene and the small, challenging-to-identify target objects. However, our approach yields a minor decline for several items, such as plates and coffee machines, in the simple kitchen scene. This may be improved by predicting scene complexity in real time during navigation. More results and analysis can be found in Appendix E and F.

Table 3. Comparison with SOTA methods on the AI2-Thor [20] / RoboTHOR [8] datasets. X indicates unacceptable resource consumption.

ID	Method			ALL (%)			Episode Time (s)↓
	Method	SR↑	SPL↑	SSR↑	NSR↑	NSNPL↑	
Ţ	SSCNav [23]	77.14 / 38.12	31.09 / 14.10	89.14 / 61.37	86.54 / 62.13	51.72 / 35.14	1.342 / 4.145 X
1	PONI [32]	78.58 / 38.42	33.78 / 16.30	89.48 / 58.46	87.81 / 65.72	52.39 / 39.83	1.591 / 4.582 X
II	OMT [14]	71.13 / 32.17	37.27 / 20.09	93.17 / 61.77	76.34 / 52.08	41.36 / 24.51	0.645 / 2.011
11	VGM [21]	73.95 / 35.82	40.69 / 23.71	94.42 / 62.93	78.32 / 56.92	42.62 / 25.80	0.731 / 2.458
	ORG [10]	67.32 / 30.51	37.01 / 18.62	91.07 / 59.64	73.88 / 51.15	40.24 / 20.64	0.241 / 0.769
III	HOZ [41]	68.53 / 31.67	37.50 / 19.02	91.44 / 60.11	74.94 / 52.68	40.83 / 21.02	0.283 / 0.808
111	VTNet [11]	72.24 / 33.92	44.57 / 23.88	94.18 / 63.29	76.62 / 53.59	46.74 / 28.26	0.321 / 1.325
	DOA [6]	74.32 / 36.22	40.27 / 22.12	95.73 / 64.18	77.63 / 56.43	44.11 / 25.88	0.334 / 1.247
IV	Ours (DAT)	82.39 / 41.72	48.93 / 27.91	97.25 / 67.24	84.71 / 62.04	50.32 / 34.27	0.352 / 1.211

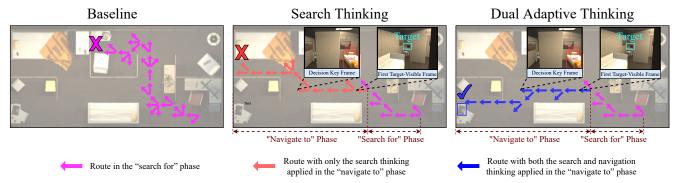


Figure 6. We show the navigation routes of three different models to complete the same task in the same environment. The baseline (ORG [10]) fails to navigate in the "search for" phase. The search thinking method (DOA [6]) and our DAT method diverge at the decision key frame in the "navigate to" phase. The navigation routes in more scenarios are shown in Appendix G.

5.4. Comparisons with the State-of-the-Art

Our DAT method is compared with three categories of relevant SOTA methods, as shown in Table 3. (I) Modular methods based on active SLAM. An agent with a semantic map can directly use the path planning method to quickly navigate to the target after locating it; thus, these methods obtain a higher NSNPL. Nevertheless, these methods require considerable efforts to explore the environment which makes finding targets ineffective. The SPL of the current state-of-the-art modular method PONI [32] is 15.15/11.61 lower (AI2-Thor/RoboTHOR, %) than that of our DAT method. More seriously, maintaining the semantic map at all times causes each step to consume several times as long as our method. (II) Long-term memory methods. These methods theoretically depend on historical information to model environments more clearly; however, methods such as OMT [14] and VGM [21] store overcomplicated features, increasing the difficulty of network learning. Therefore, the current memory modules do not exert their full strength. (III) Search thinking methods. These methods enhance search capabilities through object association. Compared to the best search thinking model DOA [6], our DAT model brings 8.07/5.50, 8.66/5.79 and 6.21/8.39 improvements in SR, SPL and NSNPL (AI2-Thor/RoboTHOR, %). More experiments are in Appendix D.

5.5. Qualitative Analysis

Routes of different methods are visualized in Figure 6. The baseline model is stuck in the wrong room due to its limited capability to search for targets. The search thinking model is disturbed by extraneous objects in the "navigate to" phase, leading it to choose the wrong direction at the keyframe. In contrast, our DAT method chooses the appropriate left room based on the representation of the target relative position generated by navigation thinking.

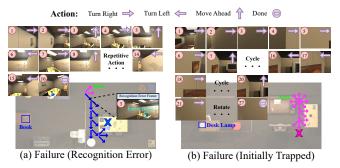


Figure 7. Failure cases with the first-person views. For brevity, the camera's up-and-down motion has been omitted.

6. Limitations and Failure Cases

Some potential limitations are observed in testing. (i) The model is sensitive to object detection accuracy (Figure 7(a)). How to improve the robustness to error recognition is worth exploring. (ii) The agent sometimes gets stuck in narrow and complex initial environments without historical information (Figure 7(b)). Endowing agents with the ability to escape from the deadlock in end-to-end learning may be the key to solving this problem and we leave this for future works.

7. Conclusion

In this paper, we propose the dual adaptive thinking (DAT) method, such innovation enables agents to efficiently and reliably reach the target position after locating the target. Dual thinking includes the search thinking responsible for searching the target and the navigation thinking responsible for navigating to the target. Extensive experiments prove that dual adaptive thinking flexibly adjusts the thinking methods according to the navigation stage, thereby improving the success rate and navigation efficiency. It is worth noting that beyond the current object navigation task, multiple adaptive thinking can theoretically be applied to various time-series embodied AI tasks.

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Table 4. The details of dual adaptive thinking network for object navigation.

Module	Index	Input	Operation	Output
	(1)	S_t	FC+ReLU	(22×49)
	(2)	(1)	Attention Distribution	(22×49)
	(3)	(2)	Reshape+0.3Dropout	$(22 \times 7 \times 7)$
Search Thinking	(4)	$D(Q) I_t(K, V)$	Multi-head Attention ($HD = 512, NH = 8$)	$(64 \times 7 \times 7)$
	(5)	PA	FC+ReLU	(1×10)
	(6)	(5)	Repeat	$(10 \times 7 \times 7)$
	(7)	(3,4,6)	Concatenation	$(96 \times 7 \times 7)$
	(8)	TOMG	Coordinate Egocentric	(27×11)
Navigation Thinking	(9)	(8)	FC+ReLU	(27×16)
Navigation Tilliking	(10)	(9)	TAMSA ($\pounds = 3$)	(1×32)
	(11)	(10)	Repeat+0.3Dropout	$(32 \times 7 \times 7)$
	(12)	(7,11)	Concatenation+LayerNorm	$(128 \times 7 \times 7)$
Adaptive Fusion	(13)	(12)	FC+ReLU	$(64 \times 7 \times 7)$
	(14)	(13)	0.3Dropout+Flatten	3136
	(15)	(14)	Two Layers LSTM	512
Policy Learning	(16)	(15)	Actor FC	6
	(17)	(15)	Critic FC	1

Table 5. Hyperparameters during training.

Tueste et 11) per parameters during transmig.									
	penalize each step	-0.01							
Reward	encourage move ahead	+0.01							
	succeed	+5.00							
	discount factor	0.99							
A3C	lambda parameter for GAE	1.00							
ASC	entropy term coefficient	0.01							
	value loss coefficient	0.50							
Learning Rate	pretrain	0.0005							
Learning Rate	reinforcement learning	0.0001							

A. More Network Details

A.1. Simulated Environment

We discretize the scene into a 0.25m grid of navigable points. To speed up reinforcement learning training, we precompute the environmental data from the simulator for each point offline. Therefore, the agent can only move between these points. The step size is 0.25m, the yaw rotation is 45 degrees, and the pitch rotation is 30 degrees.

A.2. Model Architecture

The model architecture and key details are presented in formulas and images in the main paper. Table 4 gives more details on the input, operation, hyperparameters and feature dimensions of each layer.

The search thinking module has three branches: objects (1-3), images (4), past actions (5-6). The object branch input $S_t \in \mathbb{R}^{22 \times 262}$ is obtained by DETR [4], which encodes object appearance (class labels and bounding boxes) as well as instance relations and global contexts. The image branch

input $S_t \in \mathbb{R}^{512 \times 7 \times 7}$ uses ResNet18 [17] features, which preserve spatial relationships better than deeper features. To ensure consistent dimensions for concatenation, object features and past action features are reshaped to match image features (7×7) .

The navigation thinking module uses TOMG as input, which stores only target-related information. If an object with target confidence $cf \geq 0.4$ is visible, its related information is stored in TOMG.

A.3. Training Hyperparameters

The hyperparameters for training our DAT model are given in Table 5. We use the same reward setting as DOA [6], which has three components: (i) A small negative reward of -0.01 for each step. (ii) A positive reward of 0.01 for moving ahead. (iii) A large positive reward of 5.0 for reaching any instance of the target object category within a certain number of steps.

We set the discount factor to 0.99 to balance long-term and short-term rewards. The object navigation task is complex and hard to converge, so we use n-step bootstrapping advantage estimation by setting lambda to 1 in GAE. The entropy term coefficient and value loss coefficient in A3C are 0.01 and 0.5 respectively.

We pre-train our model with supervised learning using a learning rate of 0.0005. Then we train it with reinforcement learning using a learning rate of 0.0001.

B. Disadvantages of Single Thinking

In the introduction, we explain the problems with single thinking in the "navigate to" phase. In this section, quantitative experimental results (Table 6) are used to explain

Table 6. The performance of methods with different thinking levels in the processes of "navigate to" and "search for".

Method		Path Length	1		Success Rate		Rotation Action Rate		
Wiethou	ALL	Search	Navigate	ALL	Search	Navigate	Search	Navigate	
Single Thinking	$19.92_{\pm 0.31}$	$7.42_{\pm0.14}$	$12.50_{\pm0.21}$	$76.87\%_{\pm 0.52\%}$	$94.80\%_{\pm 0.22\%}$	$81.09\%_{\pm 1.03\%}$	$66.33\%_{\pm 0.75\%}$	$60.53\%_{\pm 0.92\%}$	
Dual Thinking	$18.26_{\pm0.20}$	$7.96{\scriptstyle\pm0.11}$	$10.30_{\pm0.18}$	$82.39\%_{\pm 1.21\%}$	$97.25\%_{\pm0.34\%}$	$84.71\%_{\pm0.82\%}$	$71.62\%_{\pm 0.79\%}$	$49.04\%_{\pm 0.66\%}$	
Human	$13.15_{\pm 0.27}$	$7.13_{\pm 0.20}$	$6.02_{\pm0.15}$	$97.14\%_{\pm 0.84\%}$	$97.22\%_{\pm 0.79\%}$	$99.92\%_{\pm 0.03\%}$	$78.88\%_{\pm0.42\%}$	$31.45\%_{\pm0.34\%}$	

in detail the navigation behavior gap between single thinking and human thinking. Moreover, how our dual adaptive thinking (DAT) approach bridges this gap is presented.

B.1. Acquisition of Data

In Table 6, we display the metrics for three different thinking. The single thinking model removes the navigation thinking module from our overall model, leaving only the search thinking module. The dual thinking model is our complete DAT model. Human thinking is based on real people tests. We invited 10 subjects to independently complete all tasks that the agent must complete in all test environments. To acquire the final human indicators, the indicators of these 10 subjects are averaged after removing the highest value and the lowest value.

We analyze three main categories of indicators: path length, success rate and rotation action rate.

- 1) The path length is the average number of steps taken by the agent to complete the test tasks. The overall path consists of two phases: "search for" phase and "navigate to" phase; the first target-visible frame is the dividing point. Therefore, the overall path length is equal to the path length of the "search for" phase plus the path length of the "navigate to" phase.
- 2) The success rate is the ratio of the agent successfully reaching the target position and outputting Done. In addition to the overall success rate, we also counted the search success rate and the navigate success rate. In particular, if the agent recognizes the target object, then the "search for" phase is successful.

3) The rotation action rate is the ratio of actions that do not change the agent's position. We counted the agent's rotation action rate in the "search for" phase and the "navigate to" phase.

B.2. Comparative Analysis of Different Thinking

In terms of the path length, the human result is 6.77 steps shorter than the single thinking method, which is attributed mainly to the gap in the "navigate to" phase. By introducing dual thinking, our DAT method significantly optimizes the route in the "navigate to" phase, and the navigation efficiency in the "search for" phase is maintained.

Regarding the success rate, the overall success rate is affected by the combination of the search success rate and the navigation success rate. The navigation success rate is increased since the dual thinking network can memorize and generate the target's approximate orientation thanks to our navigation thinking. Introducing navigation thinking has also improved the search success rate because navigation thinking shares the navigation pressure for search thinking so that search thinking can focus more on searching targets. Finally, end-to-end networks are determined to perform comparably to humans in terms of the search success rate, but there is still a significant difference in the navigation success rate. Therefore, how to improve the navigation success rate is still the main problem to be solved in the future.

Concerning the rotation and straight actions, as the thinking complexity increases, rotation actions are gradually concentrated in the "search for" phase. This trend is consistent with the different demand characteristics between

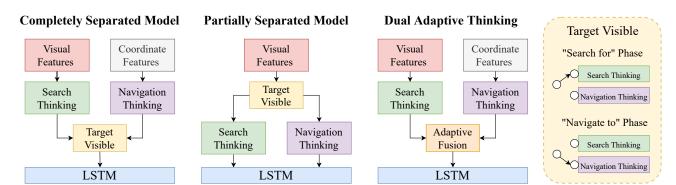


Figure 8. Different model structures for implementing dual thinking.

Table 7. Comparison with different model structures for implementing dual thinking.

Method			ALL (%)				$\mathbb{L} \geq 5$ ((%)		Episode
	SR↑	SPL↑	SSR↑	NSR↑	NSNPL↑	SR↑	SPL↑	SSR↑	NSR↑	NSNPL↑	Length↓
Partially Separated	77.49	46.61	95.68	80.99	48.26	69.48	45.62	94.97	73.66	48.14	27.19
Completely Separated	72.09	40.16	94.53	76.26	40.21	63.14	38.57	93.55	67.49	39.83	23.65
DAT (Ours)	82.39	48.93	97.25	84.71	50.32	76.21	49.32	96.22	79.20	50.14	19.87

the "search for" phase and the "navigate to" phase. In the "search for" phase, the agent needs to efficiently obtain environmental information and capture the target through abundant rotation actions. In the "navigate to" phase, the agent already knows the position of the target and needs to move forward to approach the target. The clear division of labor in each stage ensures efficient navigation.

C. Different Dual Thinking Structures

The essence of dual thinking is to use different decision networks in different navigation stages, which can be accomplished by using various model structures. As shown in Figure 8, in addition to our dual adaptive thinking (DAT) structure, we also experiment with completely and partially separated model structures.

C.1. Completely Separated Structure

The completely separated structure entirely decouples the thinking used in different stages. The difference with respect to our DAT method is that in the "navigate to" phase, the agent does not engage in search thinking and relies only on navigation thinking to make decisions. As Table 7 shows, the NSR of the completely separated structure is very low. There are two reasons for this model's failure: (1) At the beginning of the "navigate to" phase, the target information in the target-oriented memory graph (TOMG) is not sufficient to generate a complete target orientation, so it cannot independently support action decisions. (2) If no search thinking is performed, visual information will be lost, resulting in a loss of obstacle avoidance ability. Therefore, in our DAT model, search thinking is active at all times.

C.2. Partially Separated Structure

In the partially separated structure, search thinking and navigation thinking take the same input features but use different encoding networks to model the different types of thinking. The difference with respect to our DAT method is that instead of using our target-oriented coordinate features, navigation thinking relies on the same visual features as search thinking. As seen in Table 7, the performance of the partially separated structure is not ideal, especially the episode length is too long. The comparison results suggest that the presence of too much redundant information in the visual features makes it too difficult for the navigation thinking network to learn the relative position of the

target. More seriously, unreasonable navigation thinking affects the learning of the backbone visual embedding network, causing the whole model to collapse.

C.3. DAT Structure

Our DAT method uses specific input features and a reasonable adaptive fusion method for dual thinking to ensure stable and excellent network performance in different navigation stages.

D. Comparisons with the State-of-the-Art

We simply compare the aggregate metrics of all episodes due to space restrictions in the main text. However, the performance differences between various approaches cannot be completely displayed because some objects in the test set are quite close to the agent. Therefore, in Table 8 and Table 9, we supplemented the results of episodes with path lengths larger than 5 ($\mathbb{L} \geq 5$) in the two datasets. In end-to-end methods (II, III, IV), our method outperforms the SOTA method (DOA [6]) by 8.33 / 7.00, 8.96 / 4.14 in SR and SPL ($\mathbb{L} \geq 5$, AI2-Thor / RoboTHOR, %). Additionally, our approach outperforms previous end-to-end approaches during both the "search for" and the "navigate to" phases.

It is worth noting that there is no detailed navigation capability comparison between end-to-end methods (II, III, IV) and modular methods (I) in previous works. Two modular approaches (SSCNav and PONI) are transferred from the Habitat dataset to the AI2-Thor and RoboTHOR datasets in our research. Compared with the end-to-end methods, the module approaches offer clear advantages in the "navigate to" phase because of the strong interpretability of the semantic map. However, the heavy reliance on semantic mapping also results in high computing costs and inefficiencies during the "search for" phase. Therefore, modular approaches have great potential in scenarios where semantic maps can be reused repeatedly, but end-to-end approaches are still preferred in completely unknown environments.

E. Target Level Indicators

Our method has obvious advantages over other methods in terms of overall metrics. However, due to variations in navigational complexity and path characteristics between various target objects, we carried out a comparative experiment of each single target object. The findings not only deepen our understanding of the DAT method's benefits but

Table 8. Comparison with SOTA methods in AI2-Thor [20]. X indicates unacceptable resource consumption.

ID	Method	ALL (%)							$\mathbb{L} \geq 5$ (Episode	Episode	
עו	Method	SR↑	SPL↑	SSR↑	NSR↑	NSNPL↑	SR↑	SPL↑	SSR↑	NSR↑	NSNPL↑	Length↓	Time (s)↓
	Random	4.12	2.21				0.21	0.08				38.12	
т	SSCNav [23]	77.14	31.09	89.14	86.54	51.72	71.73	34.33	89.02	80.58	50.73	35.26	1.342 X
1	PONI [32]	78.58	33.78	89.48	87.81	52.39	72.92	36.40	89.13	81.81	51.82	33.64	1.591 X
II	OMT [14]	71.13	37.27	93.17	76.34	41.36	61.94	38.19	92.23	67.16	42.63	26.26	0.645
	SP [39]	68.92	38.56	91.31	75.48	40.26	52.73	33.84	89.72	58.77	35.62	27.84	0.219
	SAVN [37]	63.12	37.81	89.16	70.79	40.71	52.01	34.94	88.10	59.04	38.55	27.32	0.272
Ш	ORG [10]	67.32	37.01	91.07	73.88	40.24	58.13	35.90	90.27	64.40	38.69	26.17	0.241
111	HOZ [41]	68.53	37.50	91.44	74.94	40.83	60.27	36.61	90.31	66.74	39.82	27.24	0.283
	VTNet [11]	72.24	44.57	94.18	76.62	46.74	63.19	43.84	92.85	68.06	46.15	20.01	0.321
	DOA [6]	74.32	40.27	95.73	77.63	44.11	67.88	40.36	93.92	72.27	44.03	22.86	0.334
IV	Ours (DAT)	82.39	48.93	97.25	84.71	50.32	76.21	49.32	96.22	79.20	50.14	19.87	0.352

Table 9. Comparison with SOTA methods in RoboTHOR [8]. Xindicates unacceptable resource consumption

	Tuble 7. Companison with 5017 methods in Robo 1110R [6]. 7 medicales directly and resource consumption.												
ID	Method			ALL (%)				$\mathbb{L} \geq 5$ ((%)		Episode	Episode
110	Method	SR↑	SPL↑	SSR↑	NSR↑	NSNPL↑	SR↑	SPL↑	SSR↑	NSR↑	NSNPL↑	Length↓	Time (s)↓
	Random	0.00	0.00				0.00	0.00				0.00	
т	SSCNav [23]	38.12	14.10	61.37	62.13	35.14	33.46	11.04	60.91	54.93	33.93	106.37	4.145 X
1	PONI [32]	38.42	16.30	58.46	65.72	39.83	34.72	13.22	58.11	59.75	38.44	92.73	4.582 X
II	OMT [14]	32.17	20.09	61.77	52.08	24.51	25.33	18.16	57.35	44.17	23.82	62.99	2.011
	SP [39]	27.43	17.49	57.91	47.37	20.19	20.98	16.03	53.48	39.23	18.27	68.18	0.714
	SAVN [37]	28.97	16.59	57.23	50.62	19.55	22.89	15.21	54.84	41.74	19.14	67.22	0.812
III	ORG [10]	30.51	18.62	59.64	51.15	20.64	23.89	14.91	54.64	43.72	19.51	69.17	0.769
111	HOZ [41]	31.67	19.02	60.11	52.68	21.02	24.32	14.81	54.23	44.85	20.38	66.26	0.808
	VTNet [11]	33.92	23.88	63.29	53.59	28.26	26.77	19.80	57.72	46.38	27.50	60.27	1.325
	DOA [6]	36.22	22.12	64.18	56.43	25.88	30.16	18.32	61.39	49.13	25.11	61.24	1.247
IV	Ours (DAT)	41.72	27.91	67.24	62.04	34.27	37.16	22.46	66.13	56.19	34.10	58.81	1.211

also assess its drawbacks, offering suggestions for further study and advancement.

E.1. Experimental Setup

In the test floorplans of AI2-Thor, we initialized 8000 tasks (scene, initial position and target object) at random. We independently count the indicators (SR, SPL, SSR, NSR and NSNPL) of each target object when the agent completes these 8000 tasks. To observe how the agent performs when confronted with long path tasks, we additionally extract episodes with path lengths higher than 5. The experimental results for the DOA [6] method and our DAT method are presented in Tables 10 and Table 11, respectively.

E.2. Result Analysis

Comparison of Different Target Objects As Tables 10 and Table 11 show, the SR and SPL have a large variance on various targets, and even the gap between the maximum and minimum SR can reach more than 70%. This finding demonstrates that the navigation difficulty varies greatly as the target changes. According to the definition of SR, SSR and NSR, we obtain the following relationship:

$$SR \approx SSR \times NSR$$
 (12)

 \approx is used because there are a few instances where navigation is successful even though the target object is not recognized. Therefore, the variance fluctuation of the SR consists of the variance fluctuation of the SSR and the variance fluctuation of the NSR. Comparing the SSR column and the NSR column in Tables 10, it can be determined that the large variance of the SR is caused by the NSR and all targets achieve a high level of SSR. This indicates that the current end-to-end object navigation algorithm's difficulty is reflected primarily in the "navigate to" phase while the ability to find targets in the "search for" phase has basically matured. For example, when using the DOA method, the success rate (SR) of the most difficult target alarm clock is only 31.42%, but the success rate for the "search for" phase (SSR) has reached 99.28%. From this perspective, our DAT method is very specifically tailored to address the main shortcoming of existing end-to-end object navigation techniques.

Comparison of Different Methods Figure 9 illustrates our DAT method's influence on each target object. In the main text, we analyze the NSNPL which improves most

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obviously. In addition, NSR has also been significantly improved on various target objects. This displays that the navigation thinking we introduced not only optimizes the path of the "navigate to" phase but also substantially raises the success rate of the "navigate to" phase. Unexpectedly, our DAT approach significantly improves the SSR on only several challenging search objects and even degrades on some target objects. This phenomenon is attributed to two reasons: (i) The original DOA method has a strong target search ability through search thinking, so it is challenging to make a significant development without introducing more powerful search strategies. (ii) The search ability for each target is balanced after introducing navigation thinking and thinking adaptive fusion techniques.

Additionally, Figure 9 highlights which target objects respond best to our strategy and which ones do not. Obviously, the alarm clock and the cell phone are the two targets that our DAT method benefits the most; and of all the target objects, they are the two tiniest and hardest to locate. The difficulty in finding them is that the probability of the target recognition failing is greatly increased. Our DAT method considerably enhances the information use of each target identification by abstracting memory, which benefits small targets that are challenging to recognize. At a higher level, the differences between the different scenes are also quite obvious. The only few targets that perform poorly with our strategy are common objects in the kitchen. As discussed in the main text, the environment layout of the kitchen is relatively simple, so a simple end-to-end model sometimes works better. Therefore, we believe that it is necessary for the agent to adjust the thinking strategy in response to the perception of the environment layout. This is also a thinking direction we provide for researchers.

F. Scene Level Indicators

We discover that the contrasts between various scenes are quite clear from the analysis of each target object. Therefore, we conduct experiments on the DOA method and our DAT method in different scenes. We randomly select 1000 tasks from each scene and let the two methods complete these 1000 tasks simultaneously. The results are illustrated in Table 12.

F.1. Result Analysis

On all metrics, the bedroom scene benefits the most from our DAT method. Obviously, the bedroom is the most challenging to navigate of the four scenes. Therefore, our method is more helpful for complex and difficult scenes. Bathroom and Kitchen are two simpler scenes that require fewer steps to navigate to the target object. The optimization of our method for these two scenes is not so obvious.

G. Qualitative Results

In the main text, due to space limitations, we select only a simple scene for a qualitative analysis of navigation behavior. In Figure 10, we visualize the agent's navigation paths with different targets in four complex scenarios. We discover that when the agent needs to make a key decision, there is often no target in view. At these critical decisionmaking moments, our DAT method can provide the agent with the relative position information of the target, thereby improving the critical decision-making success rate. More significantly, our method makes each step of the agent more stable and purposeful in the "navigate to" phase. Reflecting on the navigation route, once the target has been seen, our method reduces the movement for in-situ exploration and applies more forward movement to navigate to the target position more efficiently.

H. Multiple Adaptive Thinking in Embodied ΑI

The dual adaptive thinking (DAT) network proposed in this paper provides key inspiration for future research. In object navigation tasks, dual adaptive thinking can be extended to multiple adaptive thinking. Environment modeling thinking, object state understanding thinking, and other types of thinking can be introduced in multiple adaptive thinking models. Furthermore, multiple adaptive thinking is not limited to object navigation tasks. In other embodied AI tasks, such as embodied question answering (EQA) [7] and visual language navigation (VLN) [2], agents can use multiple thinking approaches to more flexibly address real-world problems.

Table 10. The outcome of applying the DOA method with each object as the target.

DOA			ALL (%	6)				Episode			
DOA	SR↑	SPL↑	SSR↑	NSR↑	NSNPL↑	SR↑	SPL↑	SSR↑	NSR↑	NSNPL↑	Length↓
Alarm Clock	31.42	17.65	99.28	31.65	17.77	25.58	15.67	99.22	25.78	14.87	37.35
Book	54.54	27.31	84.84	64.28	31.74	44.16	25.75	80.00	55.20	31.15	25.43
Bowl	88.33	51.55	100.00	88.33	58.33	84.84	53.59	100.00	84.84	57.48	12.85
Cell Phone	48.90	25.05	86.26	56.69	32.24	35.24	20.28	79.50	44.33	23.95	33.28
Chair	63.24	33.08	98.02	64.52	31.59	53.00	32.28	97.26	54.49	31.08	26.19
Coffee Machine	91.66	53.39	100.00	91.66	53.82	87.23	57.87	100.00	87.23	54.80	12.38
Desk Lamp	78.94	42.74	93.42	84.50	49.79	69.81	42.06	90.56	77.09	46.24	17.42
Floor Lamp	54.13	27.89	95.48	56.69	29.98	49.56	28.90	94.78	52.29	30.35	27.31
Fridge	77.77	42.66	100.00	77.77	40.59	72.09	45.06	100.00	72.09	44.12	21.18
Garbage Can	69.83	44.00	96.83	72.12	45.65	65.67	44.58	96.34	68.16	45.30	21.69
Kettle	87.50	55.95	100.00	87.50	64.39	85.71	59.42	100.00	85.71	64.07	18.00
Laptop	82.49	44.33	95.72	86.19	46.84	74.28	42.12	93.71	79.26	44.59	18.07
Light Switch	82.71	47.95	97.95	83.87	53.07	75.14	50.06	98.22	76.21	50.24	17.22
Microwave	91.23	46.97	100.00	91.22	46.50	87.50	52.92	100.00	87.50	51.16	15.49
Pan	62.26	35.40	94.34	66.00	40.34	56.82	30.99	93.18	60.97	38.83	24.92
Plate	79.63	41.12	96.29	82.69	43.41	72.97	42.23	94.59	77.14	44.35	17.57
Pot	56.86	30.42	92.15	59.57	33.91	41.93	23.56	87.09	44.45	25.75	25.98
Remote Control	77.52	43.35	93.02	82.49	45.75	69.76	40.91	90.69	76.92	41.89	17.07
Sink	90.17	43.43	94.57	95.35	44.80	80.34	44.86	90.34	88.93	47.74	13.46
Stove Burner	93.49	58.89	100.00	93.49	62.92	89.19	60.55	100.00	89.19	60.34	13.11
Television	84.21	44.84	99.12	84.95	43.88	79.01	48.43	98.76	80.00	49.81	18.07
Toaster	76.19	46.00	100.00	76.19	51.56	72.72	46.83	100.00	72.72	50.43	17.16

Table 11. The outcome of applying the DAT method with each object as the target. ✓ indicates the target objects that benefit the most from our method.

DAT			ALL (%	6)				Episode			
DAI	SR↑	SPL↑	SSR↑	NSR↑	NSNPL↑	SR↑	SPL↑	SSR↑	NSR↑	NSNPL↑	Length↓
Alarm Clock √	45.00	29.22	96.43	46.67	30.37	40.31	27.22	96.12	41.94	28.27	24.79
Book	59.39	32.52	89.69	66.21	36.98	45.83	30.94	85.83	53.39	34.54	29.31
Bowl	86.66	56.08	98.33	88.13	56.94	81.81	58.51	100.00	81.82	51.65	9.98
Cell Phone ✓	68.68	32.79	90.65	75.76	39.76	57.37	28.68	86.88	66.05	34.74	27.86
Chair	67.19	36.01	98.42	68.27	35.24	58.46	36.83	97.81	59.76	36.83	20.38
Coffee Machine	93.05	49.39	97.22	95.71	51.09	91.48	56.89	95.74	95.56	59.01	15.40
Desk Lamp √	93.42	54.97	94.74	98.62	57.54	90.56	58.33	92.45	97.95	61.35	13.14
Floor Lamp ✓	54.88	34.01	93.98	58.39	38.49	52.17	35.74	93.04	56.07	40.20	26.00
Fridge ✓	88.88	47.76	100.00	88.88	50.46	90.69	52.72	100.00	90.69	56.14	17.74
Garbage Can	77.83	50.76	96.27	80.85	52.16	73.91	50.66	95.88	77.08	52.22	18.90
Kettle	93.75	61.50	100.00	93.75	68.28	92.86	60.76	100.00	92.86	68.37	18.68
Laptop	84.82	48.96	94.55	89.71	52.77	77.71	49.27	92.00	84.47	50.98	14.53
Light Switch	86.43	52.59	97.58	88.57	58.76	81.36	54.65	97.63	83.34	56.47	16.35
Microwave	96.49	55.64	100.00	96.49	53.92	95.00	60.81	100.00	95.00	59.28	12.63
Pan	47.17	28.02	92.45	51.02	33.74	43.18	27.44	90.91	47.49	31.14	24.73
Plate	79.63	44.63	100.00	79.63	42.83	72.97	41.59	100.00	72.97	43.30	17.37
Pot	50.98	30.94	90.19	56.52	37.68	32.26	83.87	83.87	38.45	24.63	30.88
Remote Control	78.29	46.25	93.02	83.34	49.90	72.09	45.68	90.69	79.49	47.72	17.01
Sink	89.00	48.63	94.86	93.66	49.30	78.27	54.22	91.03	85.98	55.62	12.79
Stove Burner	95.93	64.36	100.00	95.93	68.16	93.24	67.24	100.00	93.24	65.99	10.47
Television	80.70	45.69	98.24	82.14	47.80	74.07	47.84	97.53	75.94	49.92	14.28
Toaster	88.09	51.17	100.00	88.09	55.95	87.88	54.67	100.00	87.88	58.18	15.31

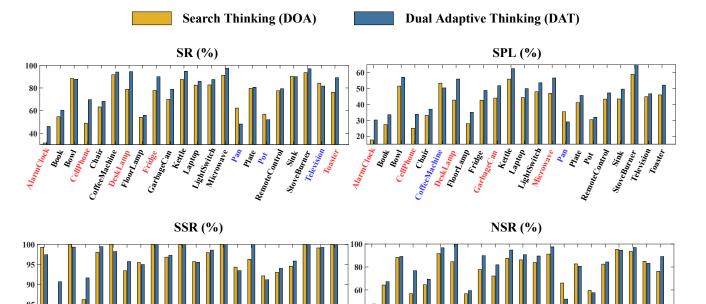


Figure 9. We analyze the SR, SPL, SSR, and SNE metrics for each object. Target objects that have greatly improved after utilizing our DAT method are shown by name in red. Target objects whose performance suffers because of applying our method are shown by name in blue.

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Remote Control

StoveBurner 1

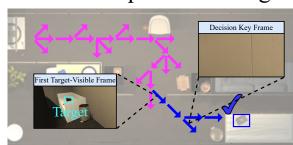
Table 12. We compare the improvement after using our DAT method in different scenes. Bold values indicate the scene that benefit the most.

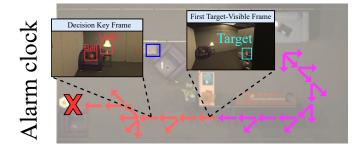
most.												
Scene	Method			ALL (%)				$\mathbb{L} \geq 5$ ((%)		Episode
Scelle	Method	SR↑	SPL↑	SSR↑	NSR↑	NSNPL↑	SR↑	SPL↑	SSR↑	NSR↑	NSNPL↑	Length↓
	DOA	69.15	38.14	95.88	72.12	39.35	61.81	37.45	94.76	65.22	38.31	23.024
Living Room	DAT	72.54	42.32	95.80	75.72	44.76	66.91	43.26	94.49	70.81	44.81	20.726
	DAT - DOA	3.39	4.18	-0.08	3.60	5.41	5.10	5.81	-0.27	5.59	6.50	-2.298
	DOA	83.89	49.30	98.78	84.82	52.41	78.76	50.96	98.34	79.94	51.72	16.817
Kitchen	DAT	86.01	52.31	98.68	87.16	53.53	82.47	54.49	98.34	83.86	53.85	16.453
	DAT - DOA	2.12	3.01	0.10	2.34	1.12	3.71	3.53	0.00	3.92	2.13	-0.364
	DOA	62.10	34.51	93.60	66.35	38.17	51.17	31.92	91.31	56.04	33.73	24.418
Bedroom	DAT	73.10	41.81	95.20	76.79	44.81	63.20	40.11	93.37	67.69	41.96	21.05
	DAT - DOA	11.00	7.30	1.60	10.44	6.64	12.03	8.19	2.06	11.65	8.23	-3.368
	DOA	87.10	45.64	95.00	91.47	48.94	78.72	48.54	92.84	84.80	51.80	13.848
Bathroom	DAT	88.90	50.34	95.10	93.48	50.98	81.12	54.49	93.04	87.19	55.03	13.582
	DAT - DOA	1.80	4.70	0.10	2.01	2.04	2.40	5.95	0.20	2.39	3.23	-0.266

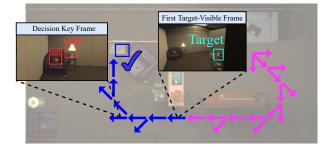
Search Thinking

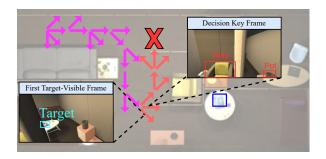
Decision Key Frame First Target-Visible Frame

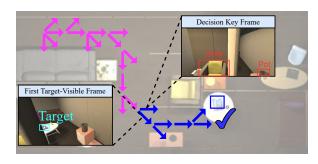
Dual Adaptive Thinking

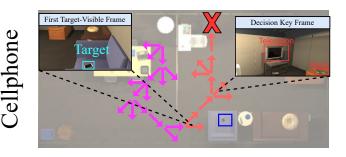












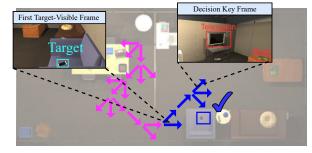


Figure 10. Visualization of navigation trajectories on the RoboTHOR dataset. The pink arrow indicates the path of the "search for" phase. The red arrow indicates the path of the "navigate to" phase when only search thinking is used. The blue arrow indicates the path of the "navigate to" phase when DAT is used.